

Dielectronic recombination of Bi^{80+} and Bi^{82+}

N. R. Badnell and M. S. Pindzola

Department of Physics, Auburn University, Auburn, Alabama 36849-5311

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We have calculated dielectronic recombination (DR) cross sections for $\Delta n=0$ transitions in Li-like Bi using the semirelativistic version of the AUTOSTRUCTURE code. We present results for the full Rydberg series associated with the $2s \rightarrow 2\bar{p}$ ($j=1/2$) core excitation, which opens up at $n=20$ and spans only 16 Ry, compared to the series associated with the $2s \rightarrow 2p$ ($j=3/2$) excitation, which opens up at $n=6$ and spans 200 Ry. We have also calculated fully relativistic and semirelativistic *KLL* DR cross sections for H-like Bi and find the effect of the Breit interaction to be important.

Experimental dielectronic recombination (DR) cross sections for highly charged ions ($Z \geq 80$) should be emerging from heavy-ion sources and storage rings in the near future.¹ In fact, high-energy ($\Delta n=1$) DR-type cross sections have already been measured² in $\text{U}^{90+} + \text{H}_2$ ion-atom collision experiments. Measurements of high-resolution low-energy ($\Delta n=0$) DR cross sections will be possible with merged electron-ion beams. We have recently³ presented results for the full Rydberg series associated with the $2s \rightarrow 2p$ ($j=3/2$) core excitation in U^{89+} and these span 350 Ry. We now present similar results for Bi^{80+} and find that they still span 200 Ry. We now also consider DR via the $2s \rightarrow 2\bar{p}$ ($j=1/2$) core excitation for which the full Rydberg series should be accessible with a relative electron-ion energy of 16 Ry in the rest frame of the ion. Returning to $\Delta n=1$ transitions, it has already been shown that the Breit interaction has a significant effect on the *KLL* resonances of He-like³ and Li-like⁴ uranium. We now show that the same is true for a highly charged H-like ion, namely Bi^{82+} .

Our theoretical methods have already been fully described.³ Our fully relativistic calculations are based on multiconfiguration Dirac-Fock wave functions with Breit and QED corrections obtained from the codes of Grant

and co-workers⁵⁻⁹ with some developments³ for the continuum part of the problem. Our semirelativistic calculations are based on the solution of the $(2j+1)$ -weighted-average single-channel Dirac equation as incorporated³ in the AUTOSTRUCTURE code.¹⁰⁻¹² Previously,³ the only two-body interaction that we included was the Coulomb electrostatic. We now look at the effect of the two-body fine-structure interactions,¹⁰ even though the Pauli approximation for the Breit interaction may not be valid¹³ and its use with the large-component solution of the Dirac equation is questionable.¹³

The reactions we consider for Bi^{80+} are

$$1s^2 2s + e^- \rightleftharpoons 1s^2 2\bar{p}nl \rightarrow \begin{cases} 1s^2 2snl + h\nu_1 \\ 1s^2 2\bar{p}n'l' + h\nu_2 \end{cases}$$

for $n \geq 20$, $n' < 20$, and $l' < n'$, and also

$$1s^2 2s + e^- \rightleftharpoons 1s^2 2pnl \rightarrow \begin{cases} 1s^2 2snl + h\nu_1 \\ 1s^2 2pn'l' + h\nu_2 \end{cases} \downarrow 1s^2 2\bar{p} + e^-$$

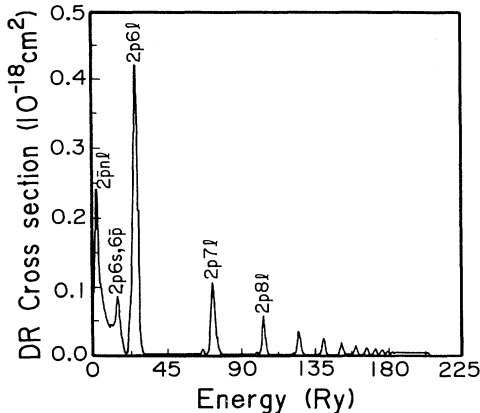


FIG. 1. Semirelativistic DR cross sections for Bi^{80+} convoluted with a 2-Ry FWHM Gaussian.

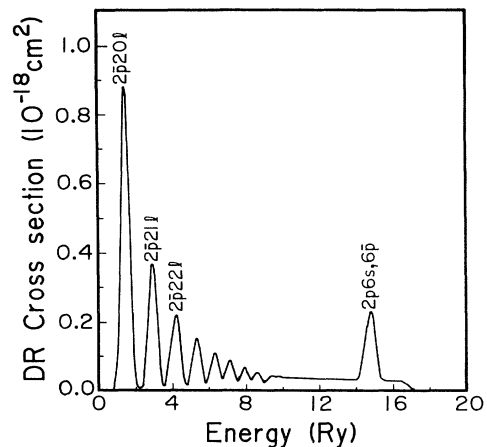


FIG. 2. Semirelativistic DR cross sections for Bi^{80+} convoluted with a 0.5-Ry FWHM Gaussian.

for $n \geq 6$, $n' < 6$, and $l' < n'$.

The reaction we consider for Bi^{82+} is

$$1s + e^- \rightleftharpoons 2l2l' \rightarrow 1s2l'' + h\nu.$$

In Fig. 1 we present our semirelativistic results for the DR of Bi^{80+} . The DR cross sections have been convoluted with a 2-Ry full width at half maximum (FWHM) Gaussian. Previously,³ we found that our semirelativistic $\Delta n = 0$ results for the DR of U^{89+} were in good agreement with our Dirac-Fock results and that the effect of the Breit interaction was negligible. The results for the $2\bar{p}nl$ series are concentrated in a narrow energy band below the $2p6l$ cross section. An expanded view of this energy region is shown in Fig. 2 for a 0.5-Ry Gaussian; only the $2p6s, 6\bar{p}$ resonances of the $2pnl$ series interlope on the $2\bar{p}nl$ series. Since we are using the isolated resonance approximation, no account is taken of any possible interference effects. We note that, as with U^{89+} , we adjusted³ our semirelativistic $2s-2p$ ($j=1/2, 3/2$) excitation energies to those calculated in the Dirac-Fock approximation with Breit and QED corrections, so that our resonances should again³ coincide with those that would have been obtained from a fully relativistic calculation.

In Fig. 3 we present the results of our fully relativistic and semirelativistic calculations for the KLL DR resonances of Bi^{82+} . We see the familiar^{3,4} three-peak structure ($2s^2, 2s2\bar{p}, 2\bar{p}^2; 2s2p, 2\bar{p}2p; 2p^2$) due to the near degeneracy of the $2\bar{p}$ and $2s$ orbital energies. Our semirelativistic results are shown both with and without the effect of two-body fine-structure interactions; they show a preferential enhancement of the lowest-energy peak, but can-

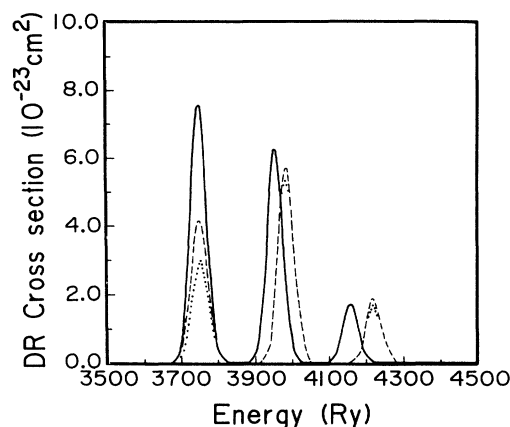


FIG. 3. DR cross section for KLL transitions in Bi^{82+} convoluted with a 50-Ry FWHM Gaussian: —, Dirac-Fock plus Breit; ···, semirelativistic with two-body Coulomb only; ---, semirelativistic with two-body Coulomb and fine structure.

not reproduce the full effect of the Breit interaction, which was included in our fully relativistic calculation.

We look forward to an experimental determination of the cross sections presented here.

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